**מבוא להצפנה – תרגיל 4**

In this capter we calculate the private key d using the extended Euclidean algorithm.

i = 0, r = 33,        s = 0, t = 1

i = 1, r = 17, q = 1, s = 1, t = 0

i = 2, r = 16, q = 1, s = -1, t = 1

i = 3, r = 1, q = 16, s = 2, t = -1

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we got that 1 = 17\*(2) + 33\*(-1)

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So:

The value of s is 2

The value of t is -1

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Now we calculate:

C\_a^s\*C\_b^t = m^(se\_a)\*m^(te\_b) = m^(se\_a + te\_b) = m (mod 16157)

Calculate 11671^-1:

First we need to calculate the inverse of 11671: 11671^-1 = 11671^-1 (mod 16157)

Now we calculate it using the extended Euclidean algorithm:

i = 0, r = 16157,        s = 0, t = 1

i = 1, r = 11671, q = 1, s = 1, t = 0

i = 2, r = 4486, q = 2, s = -1, t = 1

i = 3, r = 2699, q = 1, s = 3, t = -2

i = 4, r = 1787, q = 1, s = -4, t = 3

i = 5, r = 912, q = 1, s = 7, t = -5

i = 6, r = 875, q = 1, s = -11, t = 8

i = 7, r = 37, q = 23, s = 18, t = -13

i = 8, r = 24, q = 1, s = -425, t = 307

i = 9, r = 13, q = 1, s = 443, t = -320

i = 10, r = 11, q = 1, s = -868, t = 627

i = 11, r = 2, q = 5, s = 1311, t = -947

i = 12, r = 1, q = 2, s = -7423, t = 5362

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we got that 1 = 11671\*(-7423) + 16157\*(5362)

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So:

The value of s is -7423

The value of t is 5362

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The inverse of 11671 is -7423 (mod 16157)

11671^-1 = -7423 = 8734 (mod 16157)

Now we calculate 11671^-1 = 8734^1 (mod 16157):

using the square and multiply algorithm:

1 in binary is [1]

-----------------------------

i = 0

e\_i = 1

z^2 = 1 (mod 16157)

z\*8734 = 8734\*8734 = 8734 (mod 16157)

-----------------------------

And we got that 11671^-1 = 8734 (mod 16157)

============================

Now we calculate:

7224^2 = (mod 16157)

2 in binary is [1, 0]

-----------------------------

i = 0

e\_i = 1

z^2 = 1 (mod 16157)

z\*7224 = 7224\*7224 = 7224 (mod 16157)

-----------------------------

i = 1

e\_i = 0

z^2 = 1^2 = 15223 (mod 16157)

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And we got that 7224^2 = 15223 (mod 16157)

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The message is: 15223X8734 = 1729 (mod 16157)

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In this capter we calculate the private key d using the extended Euclidean algorithm.

i = 0, r = 33,        s = 0, t = 1

i = 1, r = 17, q = 1, s = 1, t = 0

i = 2, r = 16, q = 1, s = -1, t = 1

i = 3, r = 1, q = 16, s = 2, t = -1

-----------------

we got that 1 = 17\*(2) + 33\*(-1)

-----------------

So:

The value of s is 2

The value of t is -1

-----------------

Now we calculate:

C\_a^s\*C\_b^t = m^(se\_a)\*m^(te\_b) = m^(se\_a + te\_b) = m (mod 16157)

Calculate 11449^-1:

First we need to calculate the inverse of 11449: 11449^-1 = 11449^-1 (mod 16157)

Now we calculate it using the extended Euclidean algorithm:

i = 0, r = 16157,        s = 0, t = 1

i = 1, r = 11449, q = 1, s = 1, t = 0

i = 2, r = 4708, q = 2, s = -1, t = 1

i = 3, r = 2033, q = 2, s = 3, t = -2

i = 4, r = 642, q = 3, s = -7, t = 5

i = 5, r = 107, q = 6, s = 24, t = -17

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we got that 107 = 11449\*(24) + 16157\*(-17)

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So:

The value of s is 24

The value of t is -17

-----------------

The inverse of 11449 is 24 (mod 16157)

11449^-1 = 24 = 24 (mod 16157)

Now we calculate 11449^-1 = 24^1 (mod 16157):

using the square and multiply algorithm:

1 in binary is [1]

-----------------------------

i = 0

e\_i = 1

z^2 = 1 (mod 16157)

z\*24 = 24\*24 = 24 (mod 16157)

-----------------------------

And we got that 11449^-1 = 24 (mod 16157)

============================

Now we calculate:

13910^2 = (mod 16157)

2 in binary is [1, 0]

-----------------------------

i = 0

e\_i = 1

z^2 = 1 (mod 16157)

z\*13910 = 13910\*13910 = 13910 (mod 16157)

-----------------------------

i = 1

e\_i = 0

z^2 = 1^2 = 8025 (mod 16157)

-----------------------------

And we got that 13910^2 = 8025 (mod 16157)

============================

The message is: 8025X24 = 14873 (mod 16157)

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To check if 18 is a creator of the group Z\_349 we will calculate the following:

=============================

1. 324^0 = 5832 mod 349 = 324

2. 248^1 = 4464 mod 349 = 248

3. 276^2 = 4968 mod 349 = 276

4. 82^3 = 1476 mod 349 = 82

5. 80^4 = 1440 mod 349 = 80

6. 44^5 = 792 mod 349 = 44

7. 94^6 = 1692 mod 349 = 94

8. 296^7 = 5328 mod 349 = 296

9. 93^8 = 1674 mod 349 = 93

10. 278^9 = 5004 mod 349 = 278

11. 118^10 = 2124 mod 349 = 118

12. 30^11 = 540 mod 349 = 30

13. 191^12 = 3438 mod 349 = 191

14. 297^13 = 5346 mod 349 = 297

15. 111^14 = 1998 mod 349 = 111

16. 253^15 = 4554 mod 349 = 253

17. 17^16 = 306 mod 349 = 17

18. 306^17 = 5508 mod 349 = 306

19. 273^18 = 4914 mod 349 = 273

20. 28^19 = 504 mod 349 = 28

21. 155^20 = 2790 mod 349 = 155

22. 347^21 = 6246 mod 349 = 347

23. 313^22 = 5634 mod 349 = 313

24. 50^23 = 900 mod 349 = 50

25. 202^24 = 3636 mod 349 = 202

26. 146^25 = 2628 mod 349 = 146

27. 185^26 = 3330 mod 349 = 185

28. 189^27 = 3402 mod 349 = 189

29. 261^28 = 4698 mod 349 = 261

30. 161^29 = 2898 mod 349 = 161

31. 106^30 = 1908 mod 349 = 106

32. 163^31 = 2934 mod 349 = 163

33. 142^32 = 2556 mod 349 = 142

34. 113^33 = 2034 mod 349 = 113

35. 289^34 = 5202 mod 349 = 289

36. 316^35 = 5688 mod 349 = 316

37. 104^36 = 1872 mod 349 = 104

38. 127^37 = 2286 mod 349 = 127

39. 192^38 = 3456 mod 349 = 192

40. 315^39 = 5670 mod 349 = 315

41. 86^40 = 1548 mod 349 = 86

42. 152^41 = 2736 mod 349 = 152

43. 293^42 = 5274 mod 349 = 293

44. 39^43 = 702 mod 349 = 39

45. 4^44 = 72 mod 349 = 4

46. 72^45 = 1296 mod 349 = 72

47. 249^46 = 4482 mod 349 = 249

48. 294^47 = 5292 mod 349 = 294

49. 57^48 = 1026 mod 349 = 57

50. 328^49 = 5904 mod 349 = 328

51. 320^50 = 5760 mod 349 = 320

52. 176^51 = 3168 mod 349 = 176

53. 27^52 = 486 mod 349 = 27

54. 137^53 = 2466 mod 349 = 137

55. 23^54 = 414 mod 349 = 23

56. 65^55 = 1170 mod 349 = 65

57. 123^56 = 2214 mod 349 = 123

58. 120^57 = 2160 mod 349 = 120

59. 66^58 = 1188 mod 349 = 66

60. 141^59 = 2538 mod 349 = 141

61. 95^60 = 1710 mod 349 = 95

62. 314^61 = 5652 mod 349 = 314

63. 68^62 = 1224 mod 349 = 68

64. 177^63 = 3186 mod 349 = 177

65. 45^64 = 810 mod 349 = 45

66. 112^65 = 2016 mod 349 = 112

67. 271^66 = 4878 mod 349 = 271

68. 341^67 = 6138 mod 349 = 341

69. 205^68 = 3690 mod 349 = 205

70. 200^69 = 3600 mod 349 = 200

71. 110^70 = 1980 mod 349 = 110

72. 235^71 = 4230 mod 349 = 235

73. 42^72 = 756 mod 349 = 42

74. 58^73 = 1044 mod 349 = 58

75. 346^74 = 6228 mod 349 = 346

76. 295^75 = 5310 mod 349 = 295

77. 75^76 = 1350 mod 349 = 75

78. 303^77 = 5454 mod 349 = 303

79. 219^78 = 3942 mod 349 = 219

80. 103^79 = 1854 mod 349 = 103

81. 109^80 = 1962 mod 349 = 109

82. 217^81 = 3906 mod 349 = 217

83. 67^82 = 1206 mod 349 = 67

84. 159^83 = 2862 mod 349 = 159

85. 70^84 = 1260 mod 349 = 70

86. 213^85 = 3834 mod 349 = 213

87. 344^86 = 6192 mod 349 = 344

88. 259^87 = 4662 mod 349 = 259

89. 125^88 = 2250 mod 349 = 125

90. 156^89 = 2808 mod 349 = 156

91. 16^90 = 288 mod 349 = 16

92. 288^91 = 5184 mod 349 = 288

93. 298^92 = 5364 mod 349 = 298

94. 129^93 = 2322 mod 349 = 129

95. 228^94 = 4104 mod 349 = 228

96. 265^95 = 4770 mod 349 = 265

97. 233^96 = 4194 mod 349 = 233

98. 6^97 = 108 mod 349 = 6

99. 108^98 = 1944 mod 349 = 108

100. 199^99 = 3582 mod 349 = 199

101. 92^100 = 1656 mod 349 = 92

102. 260^101 = 4680 mod 349 = 260

103. 143^102 = 2574 mod 349 = 143

104. 131^103 = 2358 mod 349 = 131

105. 264^104 = 4752 mod 349 = 264

106. 215^105 = 3870 mod 349 = 215

107. 31^106 = 558 mod 349 = 31

108. 209^107 = 3762 mod 349 = 209

109. 272^108 = 4896 mod 349 = 272

110. 10^109 = 180 mod 349 = 10

111. 180^110 = 3240 mod 349 = 180

112. 99^111 = 1782 mod 349 = 99

113. 37^112 = 666 mod 349 = 37

114. 317^113 = 5706 mod 349 = 317

115. 122^114 = 2196 mod 349 = 122

116. 102^115 = 1836 mod 349 = 102

117. 91^116 = 1638 mod 349 = 91

118. 242^117 = 4356 mod 349 = 242

119. 168^118 = 3024 mod 349 = 168

120. 232^119 = 4176 mod 349 = 232

121. 337^120 = 6066 mod 349 = 337

122. 133^121 = 2394 mod 349 = 133

123. 300^122 = 5400 mod 349 = 300

124. 165^123 = 2970 mod 349 = 165

125. 178^124 = 3204 mod 349 = 178

126. 63^125 = 1134 mod 349 = 63

127. 87^126 = 1566 mod 349 = 87

128. 170^127 = 3060 mod 349 = 170

129. 268^128 = 4824 mod 349 = 268

130. 287^129 = 5166 mod 349 = 287

131. 280^130 = 5040 mod 349 = 280

132. 154^131 = 2772 mod 349 = 154

133. 329^132 = 5922 mod 349 = 329

134. 338^133 = 6084 mod 349 = 338

135. 151^134 = 2718 mod 349 = 151

136. 275^135 = 4950 mod 349 = 275

137. 64^136 = 1152 mod 349 = 64

138. 105^137 = 1890 mod 349 = 105

139. 145^138 = 2610 mod 349 = 145

140. 167^139 = 3006 mod 349 = 167

141. 214^140 = 3852 mod 349 = 214

142. 13^141 = 234 mod 349 = 13

143. 234^142 = 4212 mod 349 = 234

144. 24^143 = 432 mod 349 = 24

145. 83^144 = 1494 mod 349 = 83

146. 98^145 = 1764 mod 349 = 98

147. 19^146 = 342 mod 349 = 19

148. 342^147 = 6156 mod 349 = 342

149. 223^148 = 4014 mod 349 = 223

150. 175^149 = 3150 mod 349 = 175

151. 9^150 = 162 mod 349 = 9

152. 162^151 = 2916 mod 349 = 162

153. 124^152 = 2232 mod 349 = 124

154. 138^153 = 2484 mod 349 = 138

155. 41^154 = 738 mod 349 = 41

156. 40^155 = 720 mod 349 = 40

157. 22^156 = 396 mod 349 = 22

158. 47^157 = 846 mod 349 = 47

159. 148^158 = 2664 mod 349 = 148

160. 221^159 = 3978 mod 349 = 221

161. 139^160 = 2502 mod 349 = 139

162. 59^161 = 1062 mod 349 = 59

163. 15^162 = 270 mod 349 = 15

164. 270^163 = 4860 mod 349 = 270

165. 323^164 = 5814 mod 349 = 323

166. 230^165 = 4140 mod 349 = 230

167. 301^166 = 5418 mod 349 = 301

168. 183^167 = 3294 mod 349 = 183

169. 153^168 = 2754 mod 349 = 153

170. 311^169 = 5598 mod 349 = 311

171. 14^170 = 252 mod 349 = 14

172. 252^171 = 4536 mod 349 = 252

173. 348^172 = 6264 mod 349 = 348

174. 331^173 = 5958 mod 349 = 331

175. 25^174 = 450 mod 349 = 25

176. 101^175 = 1818 mod 349 = 101

177. 73^176 = 1314 mod 349 = 73

178. 267^177 = 4806 mod 349 = 267

179. 269^178 = 4842 mod 349 = 269

180. 305^179 = 5490 mod 349 = 305

181. 255^180 = 4590 mod 349 = 255

182. 53^181 = 954 mod 349 = 53

183. 256^182 = 4608 mod 349 = 256

184. 71^183 = 1278 mod 349 = 71

185. 231^184 = 4158 mod 349 = 231

186. 319^185 = 5742 mod 349 = 319

187. 158^186 = 2844 mod 349 = 158

188. 52^187 = 936 mod 349 = 52

189. 238^188 = 4284 mod 349 = 238

190. 96^189 = 1728 mod 349 = 96

191. 332^190 = 5976 mod 349 = 332

192. 43^191 = 774 mod 349 = 43

193. 76^192 = 1368 mod 349 = 76

194. 321^193 = 5778 mod 349 = 321

195. 194^194 = 3492 mod 349 = 194

196. 2^195 = 36 mod 349 = 2

197. 36^196 = 648 mod 349 = 36

198. 299^197 = 5382 mod 349 = 299

199. 147^198 = 2646 mod 349 = 147

200. 203^199 = 3654 mod 349 = 203

201. 164^200 = 2952 mod 349 = 164

202. 160^201 = 2880 mod 349 = 160

203. 88^202 = 1584 mod 349 = 88

204. 188^203 = 3384 mod 349 = 188

205. 243^204 = 4374 mod 349 = 243

206. 186^205 = 3348 mod 349 = 186

207. 207^206 = 3726 mod 349 = 207

208. 236^207 = 4248 mod 349 = 236

209. 60^208 = 1080 mod 349 = 60

210. 33^209 = 594 mod 349 = 33

211. 245^210 = 4410 mod 349 = 245

212. 222^211 = 3996 mod 349 = 222

213. 157^212 = 2826 mod 349 = 157

214. 34^213 = 612 mod 349 = 34

215. 263^214 = 4734 mod 349 = 263

216. 197^215 = 3546 mod 349 = 197

217. 56^216 = 1008 mod 349 = 56

218. 310^217 = 5580 mod 349 = 310

219. 345^218 = 6210 mod 349 = 345

220. 277^219 = 4986 mod 349 = 277

221. 100^220 = 1800 mod 349 = 100

222. 55^221 = 990 mod 349 = 55

223. 292^222 = 5256 mod 349 = 292

224. 21^223 = 378 mod 349 = 21

225. 29^224 = 522 mod 349 = 29

226. 173^225 = 3114 mod 349 = 173

227. 322^226 = 5796 mod 349 = 322

228. 212^227 = 3816 mod 349 = 212

229. 326^228 = 5868 mod 349 = 326

230. 284^229 = 5112 mod 349 = 284

231. 226^230 = 4068 mod 349 = 226

232. 229^231 = 4122 mod 349 = 229

233. 283^232 = 5094 mod 349 = 283

234. 208^233 = 3744 mod 349 = 208

235. 254^234 = 4572 mod 349 = 254

236. 35^235 = 630 mod 349 = 35

237. 281^236 = 5058 mod 349 = 281

238. 172^237 = 3096 mod 349 = 172

239. 304^238 = 5472 mod 349 = 304

240. 237^239 = 4266 mod 349 = 237

241. 78^240 = 1404 mod 349 = 78

242. 8^241 = 144 mod 349 = 8

243. 144^242 = 2592 mod 349 = 144

244. 149^243 = 2682 mod 349 = 149

245. 239^244 = 4302 mod 349 = 239

246. 114^245 = 2052 mod 349 = 114

247. 307^246 = 5526 mod 349 = 307

248. 291^247 = 5238 mod 349 = 291

249. 3^248 = 54 mod 349 = 3

250. 54^249 = 972 mod 349 = 54

251. 274^250 = 4932 mod 349 = 274

252. 46^251 = 828 mod 349 = 46

253. 130^252 = 2340 mod 349 = 130

254. 246^253 = 4428 mod 349 = 246

255. 240^254 = 4320 mod 349 = 240

256. 132^255 = 2376 mod 349 = 132

257. 282^256 = 5076 mod 349 = 282

258. 190^257 = 3420 mod 349 = 190

259. 279^258 = 5022 mod 349 = 279

260. 136^259 = 2448 mod 349 = 136

261. 5^260 = 90 mod 349 = 5

262. 90^261 = 1620 mod 349 = 90

263. 224^262 = 4032 mod 349 = 224

264. 193^263 = 3474 mod 349 = 193

265. 333^264 = 5994 mod 349 = 333

266. 61^265 = 1098 mod 349 = 61

267. 51^266 = 918 mod 349 = 51

268. 220^267 = 3960 mod 349 = 220

269. 121^268 = 2178 mod 349 = 121

270. 84^269 = 1512 mod 349 = 84

271. 116^270 = 2088 mod 349 = 116

272. 343^271 = 6174 mod 349 = 343

273. 241^272 = 4338 mod 349 = 241

274. 150^273 = 2700 mod 349 = 150

275. 257^274 = 4626 mod 349 = 257

276. 89^275 = 1602 mod 349 = 89

277. 206^276 = 3708 mod 349 = 206

278. 218^277 = 3924 mod 349 = 218

279. 85^278 = 1530 mod 349 = 85

280. 134^279 = 2412 mod 349 = 134

281. 318^280 = 5724 mod 349 = 318

282. 140^281 = 2520 mod 349 = 140

283. 77^282 = 1386 mod 349 = 77

284. 339^283 = 6102 mod 349 = 339

285. 169^284 = 3042 mod 349 = 169

286. 250^285 = 4500 mod 349 = 250

287. 312^286 = 5616 mod 349 = 312

288. 32^287 = 576 mod 349 = 32

289. 227^288 = 4086 mod 349 = 227

290. 247^289 = 4446 mod 349 = 247

291. 258^290 = 4644 mod 349 = 258

292. 107^291 = 1926 mod 349 = 107

293. 181^292 = 3258 mod 349 = 181

294. 117^293 = 2106 mod 349 = 117

295. 12^294 = 216 mod 349 = 12

296. 216^295 = 3888 mod 349 = 216

297. 49^296 = 882 mod 349 = 49

298. 184^297 = 3312 mod 349 = 184

299. 171^298 = 3078 mod 349 = 171

300. 286^299 = 5148 mod 349 = 286

301. 262^300 = 4716 mod 349 = 262

302. 179^301 = 3222 mod 349 = 179

303. 81^302 = 1458 mod 349 = 81

304. 62^303 = 1116 mod 349 = 62

305. 69^304 = 1242 mod 349 = 69

306. 195^305 = 3510 mod 349 = 195

307. 20^306 = 360 mod 349 = 20

308. 11^307 = 198 mod 349 = 11

309. 198^308 = 3564 mod 349 = 198

310. 74^309 = 1332 mod 349 = 74

311. 285^310 = 5130 mod 349 = 285

312. 244^311 = 4392 mod 349 = 244

313. 204^312 = 3672 mod 349 = 204

314. 182^313 = 3276 mod 349 = 182

315. 135^314 = 2430 mod 349 = 135

316. 336^315 = 6048 mod 349 = 336

317. 115^316 = 2070 mod 349 = 115

318. 325^317 = 5850 mod 349 = 325

319. 266^318 = 4788 mod 349 = 266

320. 251^319 = 4518 mod 349 = 251

321. 330^320 = 5940 mod 349 = 330

322. 7^321 = 126 mod 349 = 7

323. 126^322 = 2268 mod 349 = 126

324. 174^323 = 3132 mod 349 = 174

325. 340^324 = 6120 mod 349 = 340

326. 187^325 = 3366 mod 349 = 187

327. 225^326 = 4050 mod 349 = 225

328. 211^327 = 3798 mod 349 = 211

329. 308^328 = 5544 mod 349 = 308

330. 309^329 = 5562 mod 349 = 309

331. 327^330 = 5886 mod 349 = 327

332. 302^331 = 5436 mod 349 = 302

333. 201^332 = 3618 mod 349 = 201

334. 128^333 = 2304 mod 349 = 128

335. 210^334 = 3780 mod 349 = 210

336. 290^335 = 5220 mod 349 = 290

337. 334^336 = 6012 mod 349 = 334

338. 79^337 = 1422 mod 349 = 79

339. 26^338 = 468 mod 349 = 26

340. 119^339 = 2142 mod 349 = 119

341. 48^340 = 864 mod 349 = 48

342. 166^341 = 2988 mod 349 = 166

343. 196^342 = 3528 mod 349 = 196

344. 38^343 = 684 mod 349 = 38

345. 335^344 = 6030 mod 349 = 335

346. 97^345 = 1746 mod 349 = 97

347. 1^346 = 18 mod 349 = 1

348. 18^347 = 324 mod 349 = 18

=============================

The group is:

[18, 324, 248, 276, 82, 80, 44, 94, 296, 93, 278, 118, 30, 191, 297, 111, 253, 17, 306, 273, 28, 155, 347, 313, 50, 202, 146, 185, 189, 261, 161, 106, 163, 142, 113, 289, 316, 104, 127, 192, 315, 86, 152, 293, 39, 4, 72, 249, 294, 57, 328, 320, 176, 27, 137, 23, 65, 123, 120, 66, 141, 95, 314, 68, 177, 45, 112, 271, 341, 205, 200, 110, 235, 42, 58, 346, 295, 75, 303, 219, 103, 109, 217, 67, 159, 70, 213, 344, 259, 125, 156, 16, 288, 298, 129, 228, 265, 233, 6, 108, 199, 92, 260, 143, 131, 264, 215, 31, 209, 272, 10, 180, 99, 37, 317, 122, 102, 91, 242, 168, 232, 337, 133, 300, 165, 178, 63, 87, 170, 268, 287, 280, 154, 329, 338, 151, 275, 64, 105, 145, 167, 214, 13, 234, 24, 83, 98, 19, 342, 223, 175, 9, 162, 124, 138, 41, 40, 22, 47, 148, 221, 139, 59, 15, 270, 323, 230, 301, 183, 153, 311, 14, 252, 348, 331, 25, 101, 73, 267, 269, 305, 255, 53, 256, 71, 231, 319, 158, 52, 238, 96, 332, 43, 76, 321, 194, 2, 36, 299, 147, 203, 164, 160, 88, 188, 243, 186, 207, 236, 60, 33, 245, 222, 157, 34, 263, 197, 56, 310, 345, 277, 100, 55, 292, 21, 29, 173, 322, 212, 326, 284, 226, 229, 283, 208, 254, 35, 281, 172, 304, 237, 78, 8, 144, 149, 239, 114, 307, 291, 3, 54, 274, 46, 130, 246, 240, 132, 282, 190, 279, 136, 5, 90, 224, 193, 333, 61, 51, 220, 121, 84, 116, 343, 241, 150, 257, 89, 206, 218, 85, 134, 318, 140, 77, 339, 169, 250, 312, 32, 227, 247, 258, 107, 181, 117, 12, 216, 49, 184, 171, 286, 262, 179, 81, 62, 69, 195, 20, 11, 198, 74, 285, 244, 204, 182, 135, 336, 115, 325, 266, 251, 330, 7, 126, 174, 340, 187, 225, 211, 308, 309, 327, 302, 201, 128, 210, 290, 334, 79, 26, 119, 48, 166, 196, 38, 335, 97, 1, 18]

The duplicates are: [18]

- The length of the group is: 349

- The length of the group without duplicates is: 348

YES 18 is a creator of the group Z\_349

a = |G|

We are going to find the value of k such that ord(18^k) = 348 (mod 349)

We are going to find that by the formula: ord(a^k) = |G|/gcd(k, |G|)

-----------------------------------

k = 2

18^k = 18^2 = 324

gcd(k, 348) = 2

ord(18^k) = ord(18^2) = 174

-----------------------------------

k = 3

18^k = 18^3 = 80

gcd(k, 348) = 3

ord(18^k) = ord(18^3) = 116

-----------------------------------

k = 4

18^k = 18^4 = 313

gcd(k, 348) = 4

ord(18^k) = ord(18^4) = 87

-----------------------------------

k = 5

18^k = 18^5 = 168

gcd(k, 348) = 1

ord(18^k) = ord(18^5) = 348

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The value of k is: 5, and the order of 18^5 is: 348 (mod 349)

===================================

b = 29

We are going to find the value of k such that ord(18^k) = 29 (mod 349)

We are going to find that by the formula: ord(a^k) = |G|/gcd(k, |G|)

-----------------------------------

k = 2

18^k = 18^2 = 324

gcd(k, 348) = 2

ord(18^k) = ord(18^2) = 174

-----------------------------------

k = 3

18^k = 18^3 = 80

gcd(k, 348) = 3

ord(18^k) = ord(18^3) = 116

-----------------------------------

k = 4

18^k = 18^4 = 313

gcd(k, 348) = 4

ord(18^k) = ord(18^4) = 87

-----------------------------------

k = 5

18^k = 18^5 = 168

gcd(k, 348) = 1

ord(18^k) = ord(18^5) = 348

-----------------------------------

k = 6

18^k = 18^6 = 313

gcd(k, 348) = 6

ord(18^k) = ord(18^6) = 58

-----------------------------------

k = 7

18^k = 18^7 = 301

gcd(k, 348) = 1

ord(18^k) = ord(18^7) = 348

-----------------------------------

k = 8

18^k = 18^8 = 171

gcd(k, 348) = 4

ord(18^k) = ord(18^8) = 87

-----------------------------------

k = 9

18^k = 18^9 = 224

gcd(k, 348) = 3

ord(18^k) = ord(18^9) = 116

-----------------------------------

k = 10

18^k = 18^10 = 88

gcd(k, 348) = 2

ord(18^k) = ord(18^10) = 174

-----------------------------------

k = 11

18^k = 18^11 = 41

gcd(k, 348) = 1

ord(18^k) = ord(18^11) = 348

-----------------------------------

k = 12

18^k = 18^12 = 280

gcd(k, 348) = 12

ord(18^k) = ord(18^12) = 29

-----------------------------------

===================================

The value of k is: 12, and the order of 18^12 is: 29 (mod 349)

===================================